## Hints for exercises in chapter 15

Exercise 15.2.6(d). Proceed by induction, using the recursion in (c).

Exercise 15.7.1 Consider the sequence  $0, a_1, a_1 + a_2, \ldots, a_1 + \cdots + a_n \pmod{n}$ , and use the pigeonhole principle.

Exercise 15.7.3 Remove the first greedily constructed increasing subsequence starting with  $a_1$ , so the second term is  $a_r$ , where r is the minimal integer for which  $a_r > a_1$ . Suppose this has length  $\ell$ . If the remaining subsequence has parameters m', n' show that  $n \ge n' + 1$  and  $m \ge \max\{m', \ell\}$ . Then complete the proof by an induction hypothesis.