MATH 103. SECTION 205. QUIZ 1A FEBRUARY 1ST, 2007

NAME:

STUDENT NUMBER:

1. Find the area enclosed between the graphs of x^2 and x + 2 using integrals and the Fundamental Theorem of Calculus.

Solution: We look for the intersection of graphs. We need to solve

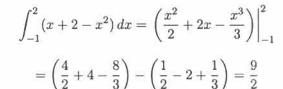
$$x^2 = x + 2.$$

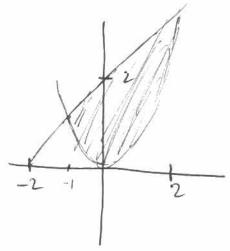
So,

$$x^2 - x - 2 = 0$$

$$(x+1)(x-2) = 0$$

Therefore, the graphs intersect at x = -1 and x = 2. We need to compute





2. Compute the following integrals using the Fundamental Theorem of Calculus.

a.

$$\int_0^{\frac{\pi}{2}} \cos(5x) \, dx = \left. \frac{\sin(5x)}{5} \right|_0^{\frac{\pi}{2}} = \frac{1}{5} - \frac{0}{5} = \frac{1}{5}$$

b.

$$\int_{-2}^{1} 2e^{3x} \, dx = \left. 2 \frac{e^{3x}}{3} \right|_{-2}^{1} = \frac{2e^{3}}{3} - \frac{2e^{-6}}{3} = \frac{2(e^{3} - e^{-6})}{3}$$

e:

$$\int_0^1 x^2 (1-x) \, dx = \int_0^1 (x^2 - x^3) \, dx = \frac{x^3}{3} - \frac{x^4}{4} \Big|_0^1 = \frac{1}{3} - \frac{1}{4} = \frac{1}{12}$$

MATH 103. SECTION 205. QUIZ 1B FEBRUARY 1ST, 2007

NAME:

STUDENT NUMBER:

1. Find the area enclosed between the graphs of x^2 and 2-x using integrals and the Fundamental Theorem of Calculus.

Solution: We look for the intersection of graphs. We need to solve

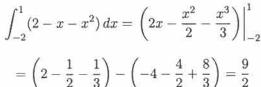
$$x^2 = 2 - x.$$

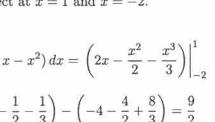
So

$$x^2 + x - 2 = 0$$

$$(x-1)(x+2) = 0$$

Therefore, the graphs intersect at x = 1 and x = -2. We need to compute







a.

$$\int_0^{\frac{\pi}{2}} \cos(9x) \, dx = \frac{\sin(9x)}{9} \Big|_0^{\frac{\pi}{2}} = \frac{1}{9} - \frac{0}{9} = \frac{1}{9}$$

b.

$$\int_{1}^{2} 2e^{3x} dx = 2\frac{e^{3x}}{3} \bigg|_{1}^{2} = \frac{2e^{6}}{3} - \frac{2e^{-3}}{3} = \frac{2(e^{6} - e^{-3})}{3}$$

C.

$$\int_0^1 x(1-x^2) \, dx = \int_0^1 (x-x^3) \, dx = \frac{x^2}{2} - \frac{x^4}{4} \Big|_0^1 = \frac{1}{2} - \frac{1}{4} = \frac{1}{4}$$